

Name _____

/100

Each problem is worth 10 points.

Simplify the following using only positive rational exponents:

1. $\frac{(4x^{-5}y^{-3})^{-2} \cdot (\frac{1}{2}x^{-3}y^{\frac{1}{3}})^{-3}}{x^4y^{-5}} =$ _____

2. $(a^{-1} + b^{-1})^{-1} =$ _____

3. $(-27)^{-\frac{2}{3}} =$ _____

4. Express the following numbers in scientific notation as numbers between 1 and 10 times the appropriate power of 10.

a) 7,342,285 = _____

b) $0.000205 \times 10^{-6} =$ _____

c) $\frac{(200,000,000) \cdot (3.5 \times 10^{-12})}{4.00 \times 10^{-4}} =$ _____

5. Express the following using only positive rational exponents.

a) $\sqrt[4]{a^8 + b^8} =$ _____

b) $\sqrt[7]{x^2} =$ _____

Simplify the following expressing all answers in **simplest radical form**. To earn a full 10 points, you must state the answer with a rationalized denominator. **Assume** for **even** roots that all **variables** represent **positive** numbers.

6. $\sqrt{\frac{125}{8x^5}}$ = _____

7. $\frac{1}{\sqrt[3]{-16x^6y^5}}$ = _____

8. $\frac{20}{2-\sqrt{2}} - 2\sqrt{50}$ = _____

9. Simplify the following complex number, expressing the result in standard $(a + bi)$ form .

$$\frac{9+\sqrt{-81}}{3+2i} - (\sqrt{25} - \sqrt{-16}) = \underline{\hspace{2cm}}$$

10. Find all real solutions of the following equation. $\sqrt{x+9} - \sqrt{x-24} = 3$